

# Hybrid Heterogeneous Electric Vehicle Routing Problem with Time Windows and recharging stations

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# Outline

- Motivation
- Hybrid Heterogeneous E-VRP with Time Windows
- Methodology
- Heuristic solver
- Experiments on preliminary benchmark instances

# Motivation – Battery Electric Vehicles (BEV)

- Eco-friendly(ier) way to travel
- Technological advances
  - extended range
  - more cost-efficient



<http://cleantechnica.com/2014/06/10/sales-nissan-e-nv200-electric-van-begin-october/>



[http://en.wikipedia.org/wiki/Tesla\\_Roadster](http://en.wikipedia.org/wiki/Tesla_Roadster)

- However

- initial cost are still high
- limited battery lifetime/cycle
- range limited
- time-consuming recharging operation
- => efficient routing required (E-VRPTW, see Schneider et al., 2014)



<http://www.citi.io/2015/04/22/cooler-cities-with-electric-vehicles/>

- Alternative: Hybrid Electric Vehicles

- combination of an internal combustion and a pure-electric engine

# Introduction – (Hybrid) Electric Vehicles

- (Full) Hybrid Electric Vehicle
  - energy generated by breaking maneuvers (recuperation)
  - used for stop&go (e.g. at traffic lights/signs) / small distances
  
- Plug-in Hybrid Electric Vehicles (PHEV)
  - two engines: internal combustion engine (ICE) and pure electric engine
  - separately rechargeable battery (recharging station)
  - on-the-fly switch between engines

# Introduction – (Hybrid) Electric Vehicles

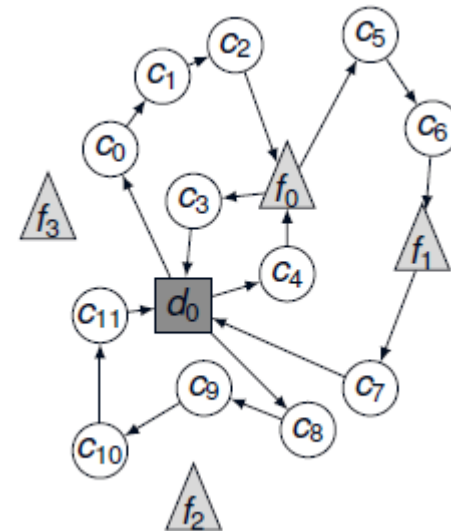
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<http://www.toyota.com/prius-plug-in-hybrid/>

# Hybrid Heterogeneous Electric Vehicle Routing Problem with Time Windows and recharging stations

- 3 vehicle classes
  - Internal Combustion Engine Vehicles (ICEV)
  - Battery Electric Vehicles (BEV)
  - Plug-in Hybrid Electric Vehicles (PHEV)
  
- 2 engine types
  - internal combustion engine
  - pure-electric engine
  
- Sub-types differing in
  - transport capacity
  - acquisition/utility cost
  - battery capacity
  - energy/fuel consumption rate

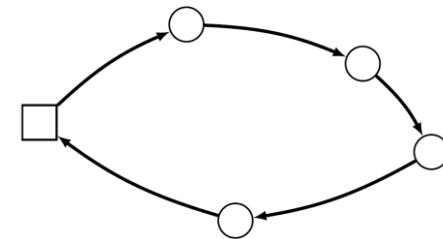


| Fossil Fuel |      | Energy |  |
|-------------|------|--------|--|
| ICEV        | PHEV | BEV    |  |

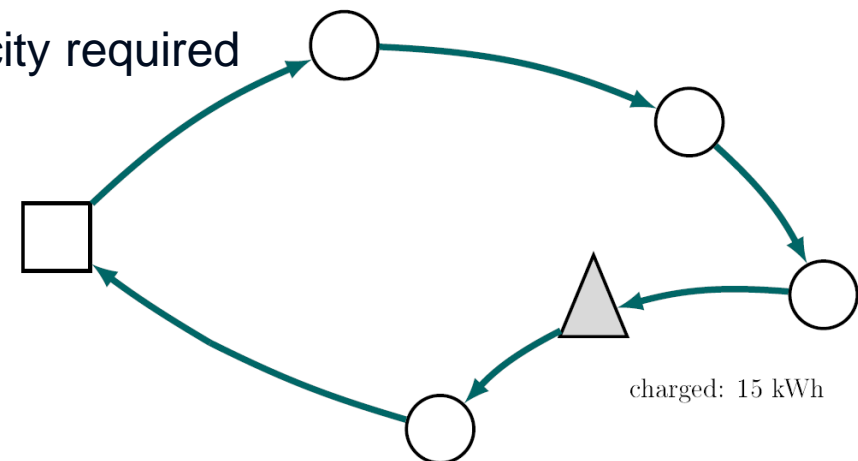


# Routing Problems

- Internal Combustion Engine Vehicles => VRPTW
  - well researched topic



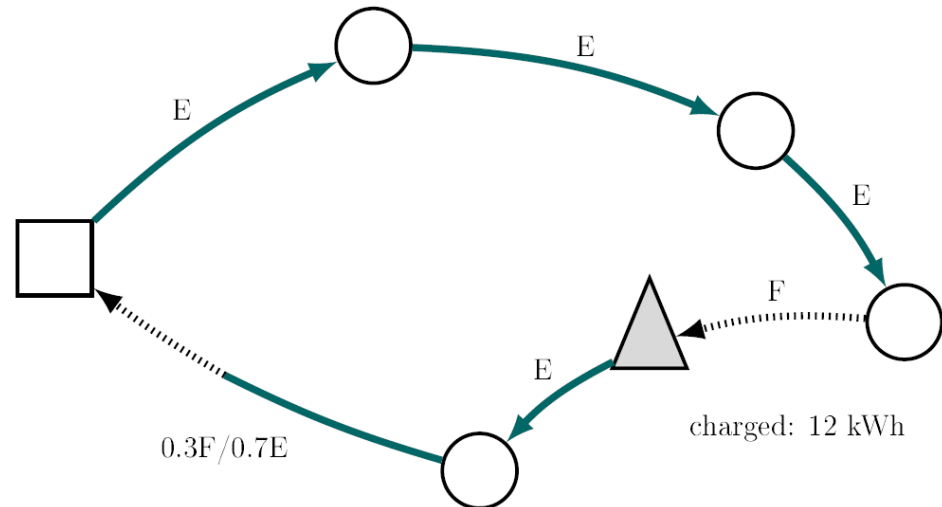
- Battery Electric Vehicles => E-VRPTW(PR)
  - visits to additional nodes (recharging stations) for recharging
  - partial recharging (PR)
    - no recharge to maximum capacity required
    - additional decision on the amount recharged per visit





# Routing Problems

- Plug-in Hybrid Electric Vehicles
  - visits to additional nodes (recharging stations) for recharging
  - partial recharging assumed as well
  - decision when to use
    - pure electric engine
    - ICE
  
- Assumption
  - use of energy is always better



# How to optimize the combined problem?

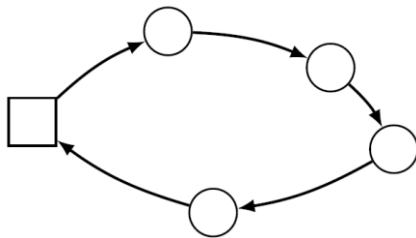
- Alternatives
  - solve each problem separately – combine them afterwards
    - + straight forward to implement
    - no combined local improvement
  - combined with problem specific operators
    - + likely to result in better solutions (no abstraction)
    - high dependency / no extendibility (very specific)

# How to optimize the combined problem?

- Our approach
  - use a layered, unifying view on the problems
    - find a common representation (top layer)
    - use optimization methods to solve specific aspects (to optimality) during evaluation (problem layers)
  
  - + smaller solution space
  - + modular design with replaceable parts
  - runtime depend heavily on the specific sub-problem solver

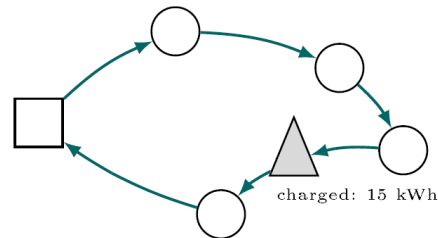
# Methodology – Decision Layers

ICEV



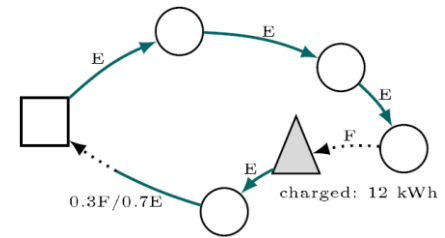
itinerary

BEV



itinerary  
RS visits  
charge in RS

PHEV

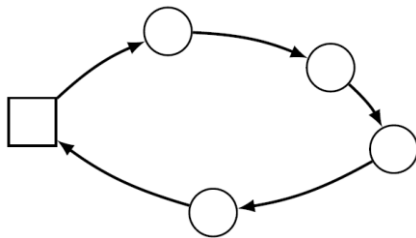


itinerary  
RS visits  
charge in RS  
mode selection

(RS .. recharging station)

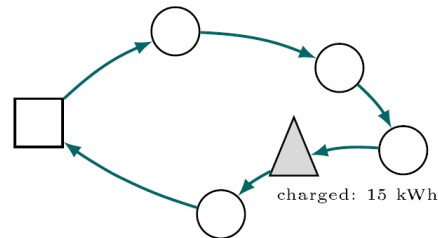
# Methodology – Decision Layers

ICEV



**itinerary**

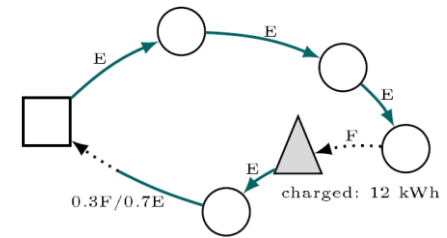
BEV



**itinerary**

RS visits  
charge in RS

PHEV

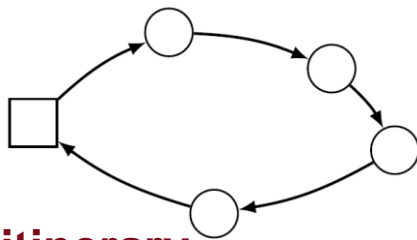


**itinerary**

RS visits  
charge in RS  
mode selection

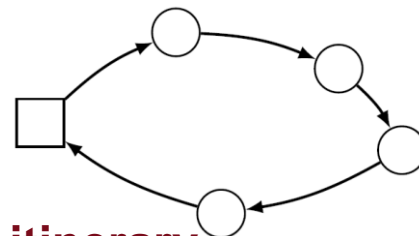
# Methodology – Decision Layers

ICEV



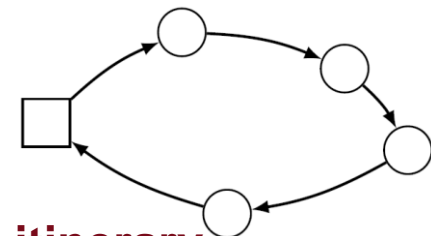
itinerary

BEV



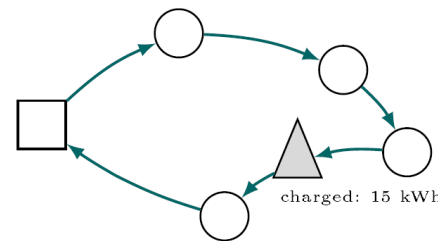
itinerary

PHEV

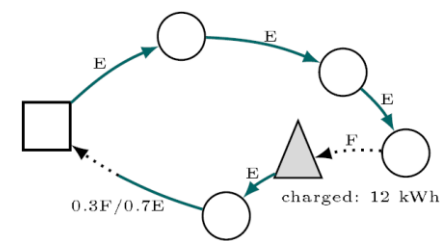


itinerary

Top Layer



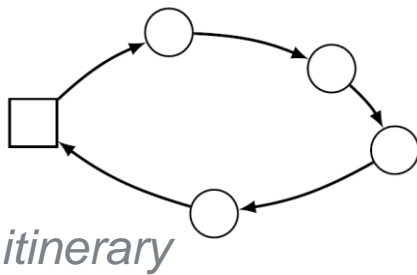
RS visits  
charge in RS



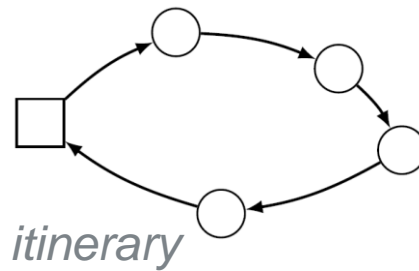
RS visits  
charge in RS  
mode selection

# Methodology – Decision Layers

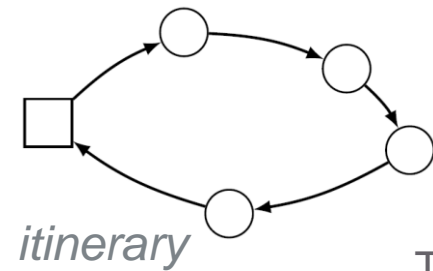
ICEV



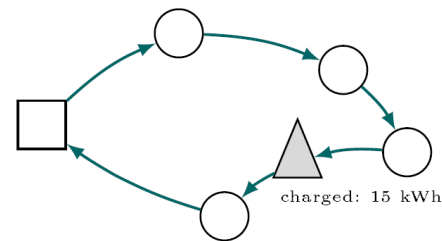
BEV



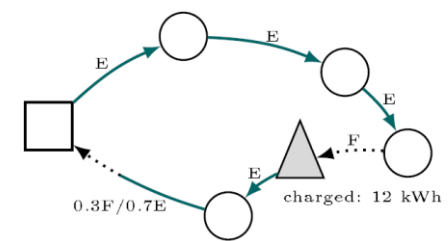
PHEV



Top Layer



**RS visits**  
charge in RS



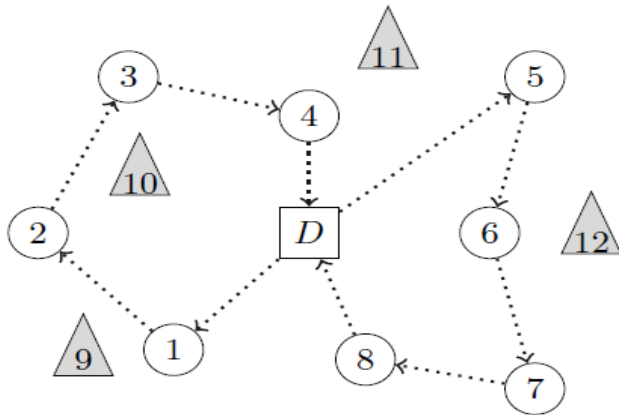
**RS visits**  
charge in RS  
mode selection

# Recharging Stations Visits

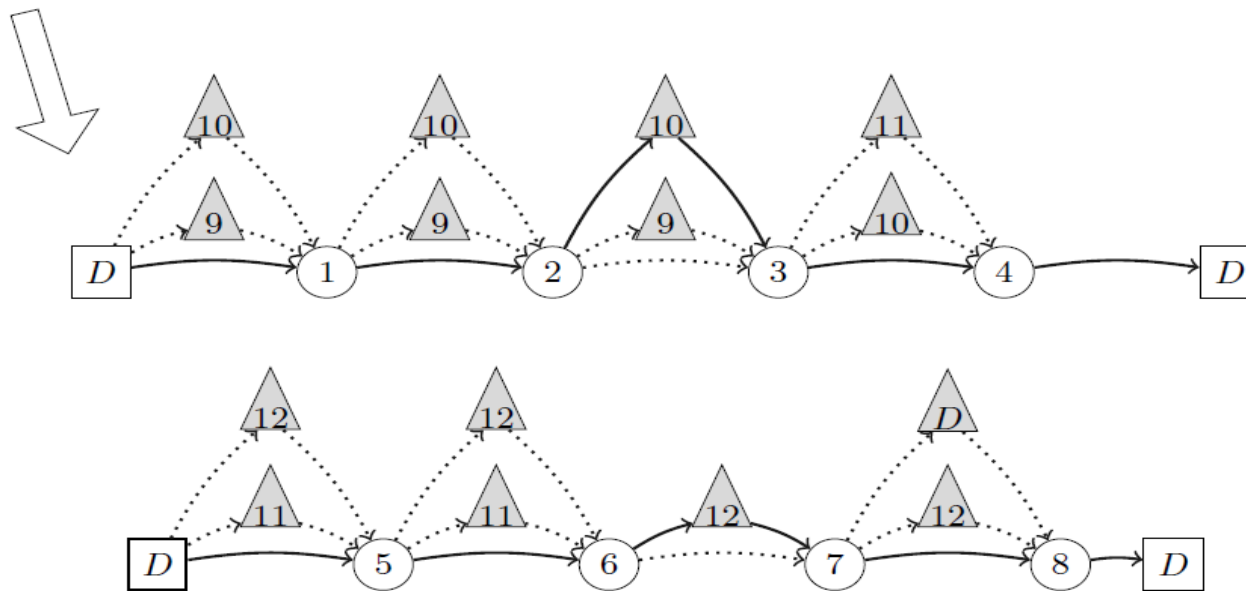
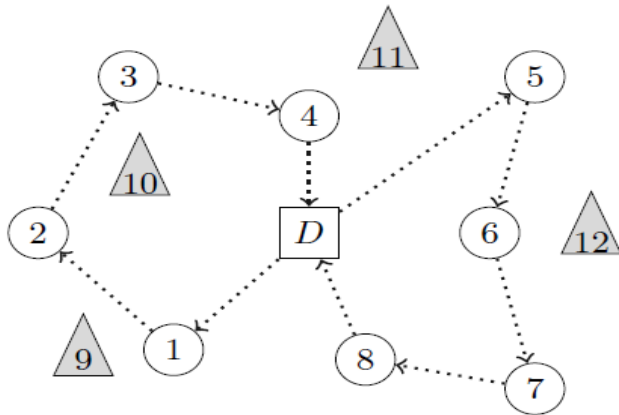
- Explicit handling of recharging stations
  - insert a recharging station (RS) node into the route explicitly
  - special operators needed to handle insertion/removal of RS
- Implicit handling of recharging stations
  - RS are inserted into an auxiliary route for evaluation only
  - mapping of VRPTW  $\leftrightarrow$  E-VRPTW
  - can be greedy or more intelligent
  - no special operators needed in the base route (VRPTW)
    - well-researched neighbourhood operators applicable
  - we use labelling for (optimal) RS insertion



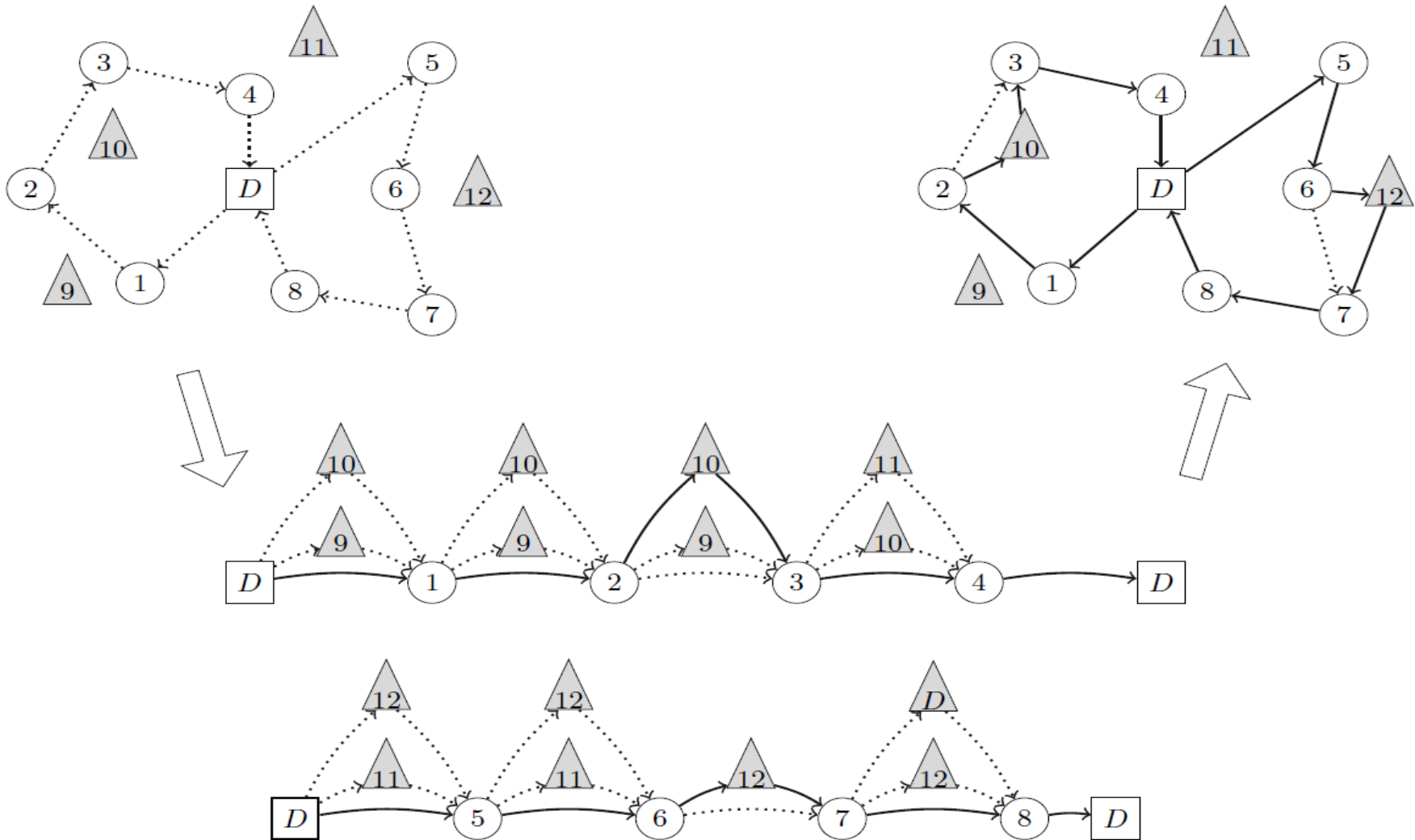
# Implicit handling of Recharging Stations



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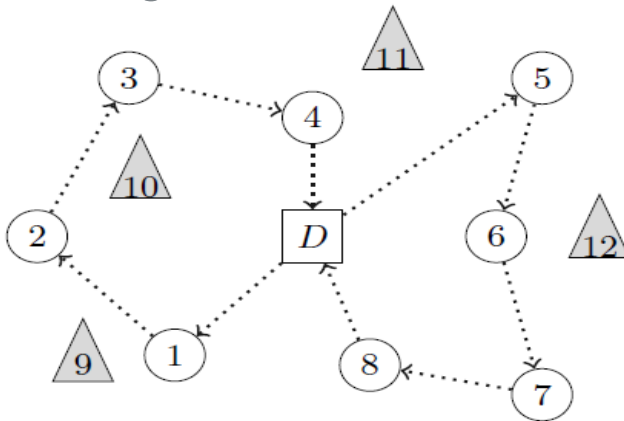


# Implicit handling of Recharging Stations



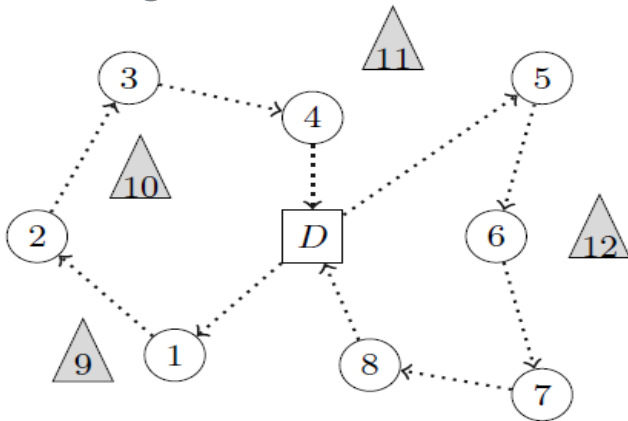
# Implicit handling of Recharging Stations

## Neighbourhood Search: Relocation Operator

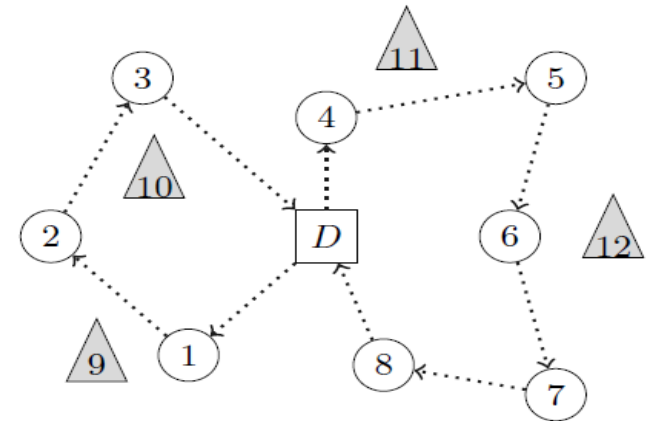


# Implicit handling of Recharging Stations

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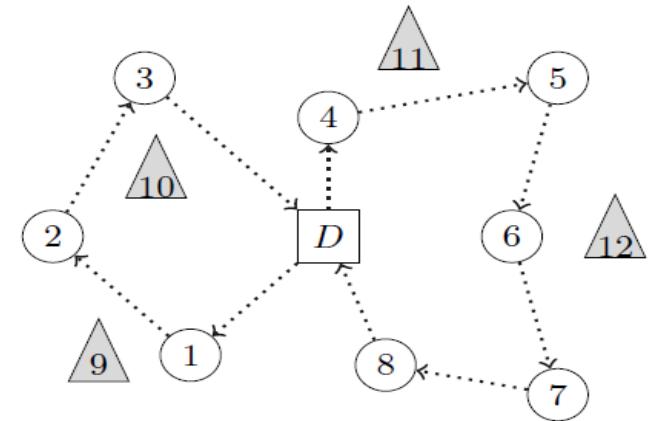
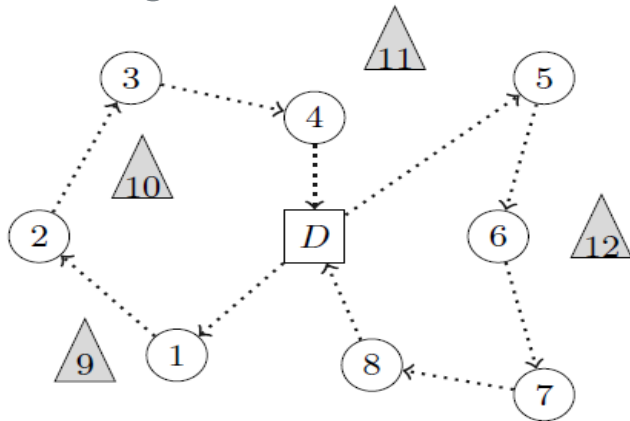


RELOCATE  
4 before 5

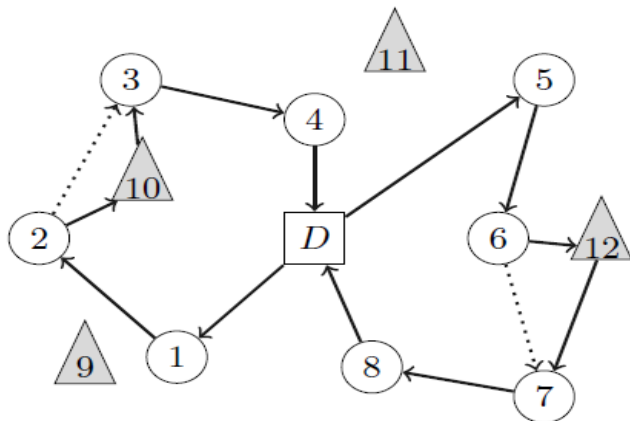


# Implicit handling of Recharging Stations

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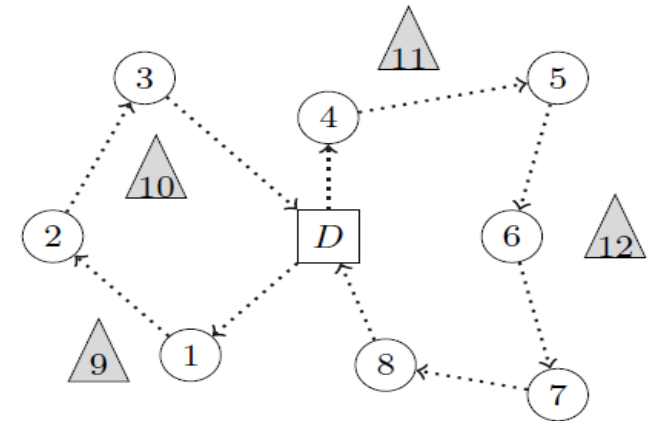
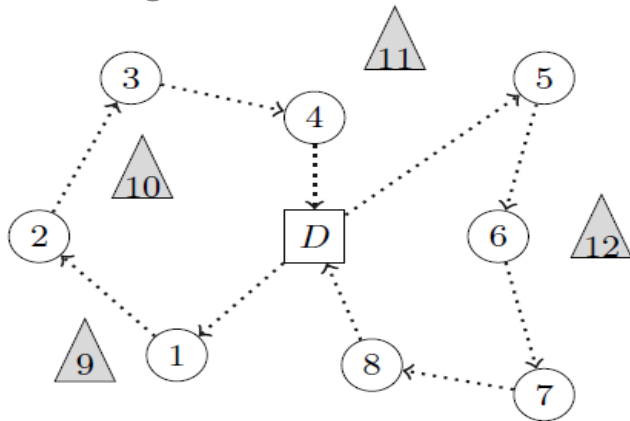


RELOCATE  
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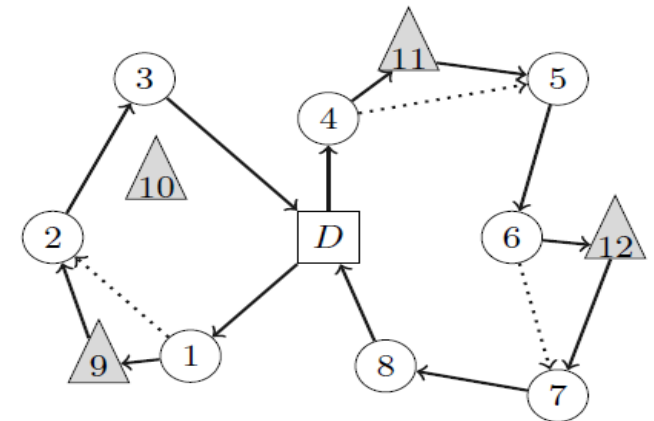
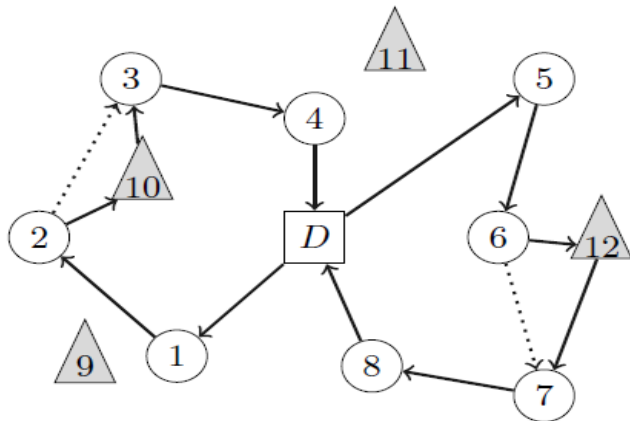


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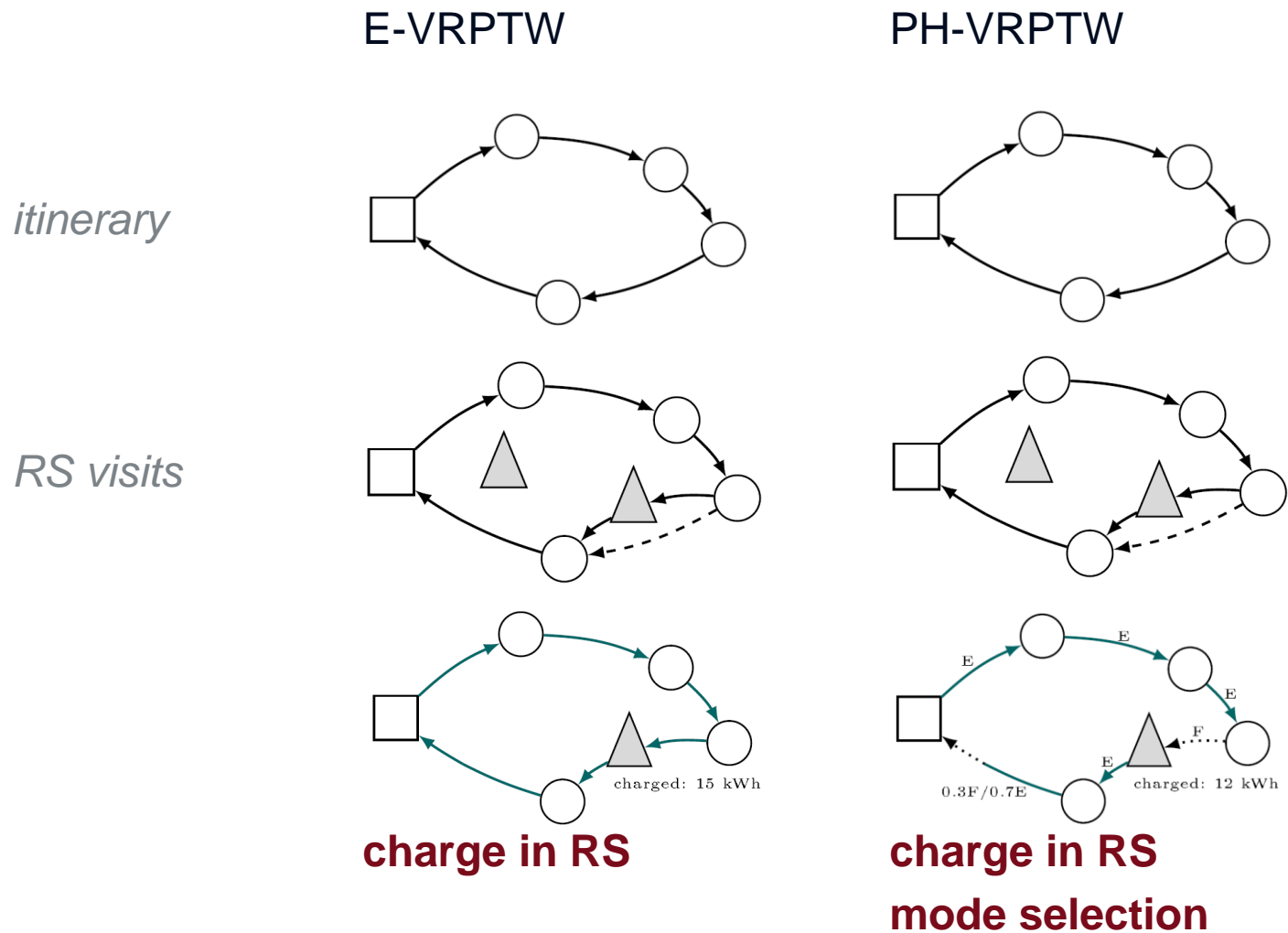
## Neighbourhood Search: Relocation Operator



RELOCATE  
4 before 5



# Methodology – Decision Layers







# Evaluation for Plug-in Hybrid Electric Vehicles

## Assumptions

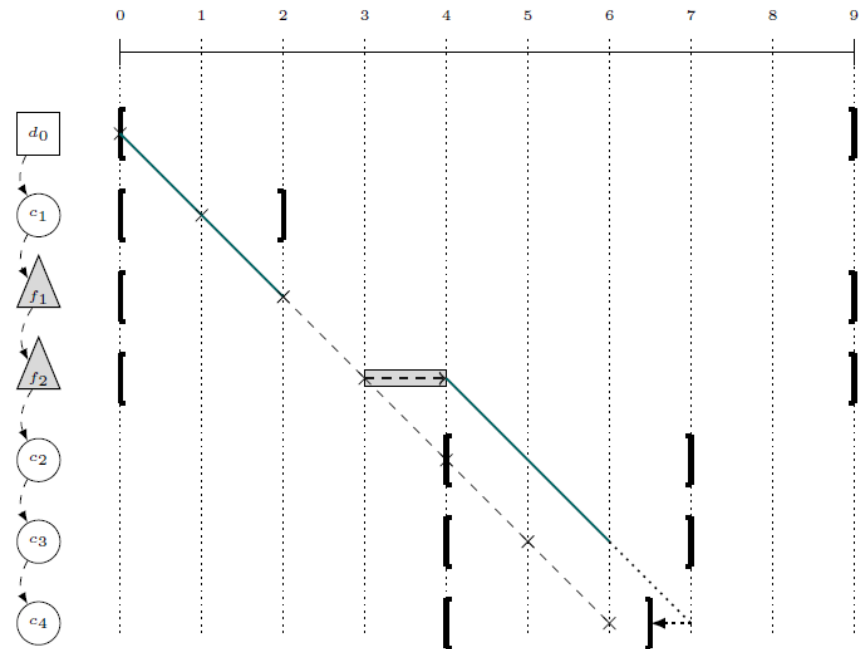
- recharging rate is linear (time)
- energy consumption is also linear (distance)
- no constraints or additional costs for mode switching

## Decision

- quantity to recharge
- which engine to use when or
- how much is energy/fuel is needed

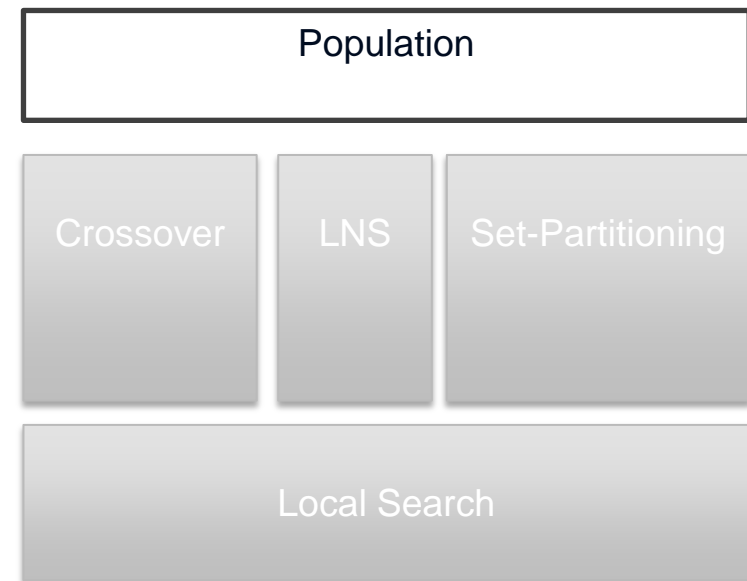
## Greedy policy

1. energy  $\leftarrow$  time (lazy recharging)
2. fuel  $\rightarrow$  time (lazy engine switch)



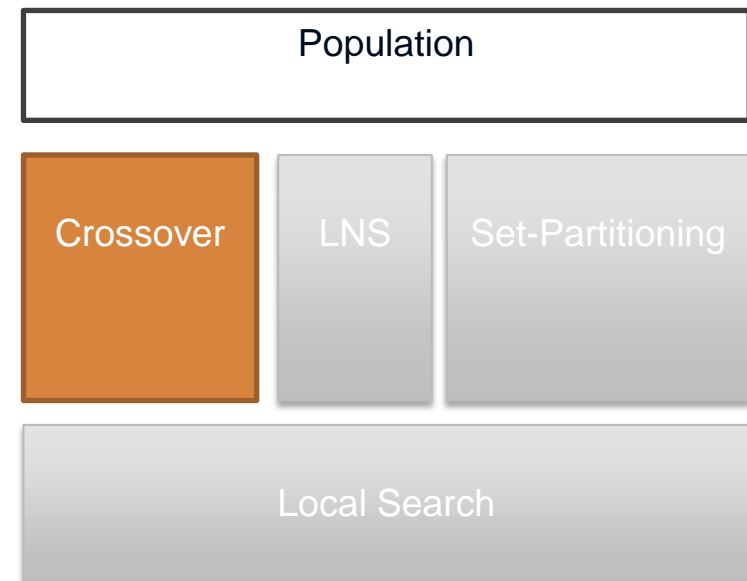
# Heuristic Solver

- Population-based Metaheuristic (Hybrid Genetic Algorithm (Vidal et al., 2013))
- Individual (Chromosome) contains of
  - giant tour without route delimiter (and recharging stations)
  - full solution (list of complete tours)
- Individual is selected using binary tournament selection
- Penalization
  - load capacity and time-window relaxation



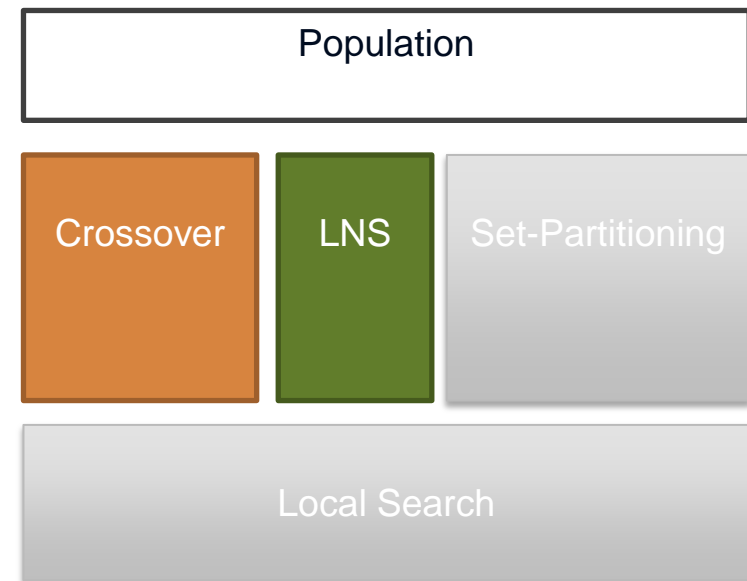
# Heuristic Solver

- Population-based Metaheuristic (Hybrid Genetic Algorithm (Vidal et al., 2013))
- Crossover
  - selecting a second Individual using Binary Tournament as well
  - Ordered Crossover (OX) on the giant tours
  - using split procedure for decoding



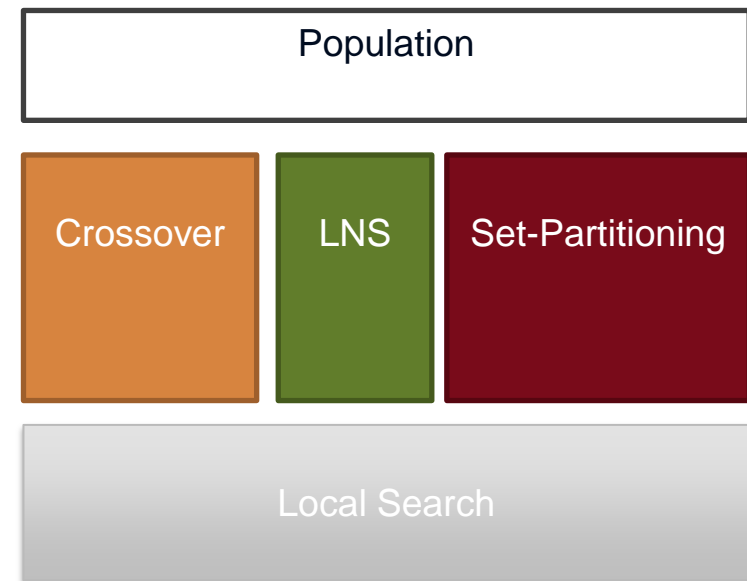
# Heuristic Solver

- Population-based Metaheuristic (Hybrid Genetic Algorithm (Vidal et al., 2013))
  
- Large Neighbourhood Search
  - set of destroy operators
    - random removal
    - similar (Shaw)
    - route removal
    - target
  - set of repair operators
    - greedy insertion
    - 2-regret insertion
  - random selection (roulette-wheel with equal probability)



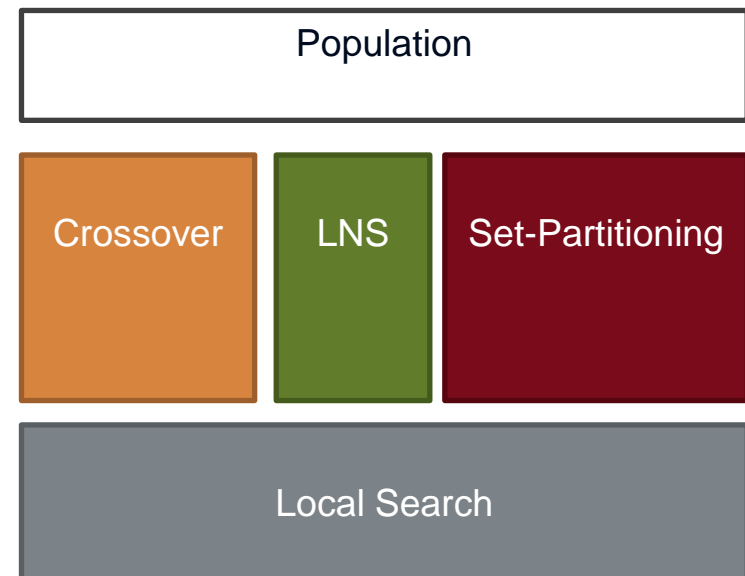
# Heuristic Solver

- Population-based Metaheuristic (Hybrid Genetic Algorithm (Vidal et al., 2013))
- Set Partitioning
  - pre-processed set of all 1-2 customer tours
  - store promising complete tours (> 2 customers) throughout the search
  - solve set partitioning problem



# Heuristic Solver

- Population-based Metaheuristic (Hybrid Genetic Algorithm (Vidal et al., 2013))
- Local Search (Education)
  - 2Opt, 2Opt\*
  - Relocate (1-2), Swap (0-2)
  - also used as a heuristic repair step (multiply penalties by 10/100)



## Preliminary Experiments – Related Benchmark

- E-FSMVRPTW instances from previous work (2014)
  - combined E-VRPTW Instances with extended Liu&Shen vehicle type definition for the FSMVRPTW
  - only BEVs
  - solved using ALNS/LS/Labelling



## Preliminary Experiments – Related Benchmark

- E-FSMVRPTW instances from previous work (2014)

| instance | H14     |         | HGA     |         | Gap     |         |
|----------|---------|---------|---------|---------|---------|---------|
|          | min     | avg     | min     | avg     | min     | avg     |
| A,B,C    |         |         |         |         |         |         |
| C1       | 3784.49 | 3796.56 | 3780.47 | 3784.13 | -0.083% | -0.389% |
| C2       | 2746.01 | 2763.62 | 2743.51 | 2743.81 | -0.088% | -0.878% |
| R1       | 2514.76 | 2544.47 | 2499.86 | 2510.40 | -0.410% | -1.226% |
| R2       | 1863.31 | 1884.47 | 1858.82 | 1863.48 | -0.208% | -1,186% |
| RC1      | 2983.82 | 3022.68 | 2972.07 | 2984.83 | -0.346% | -1.243% |
| RC2      | 2414.74 | 2437.14 | 2412.30 | 2419.19 | -0.091% | -0.842% |

## Preliminary Experiments – New Instances

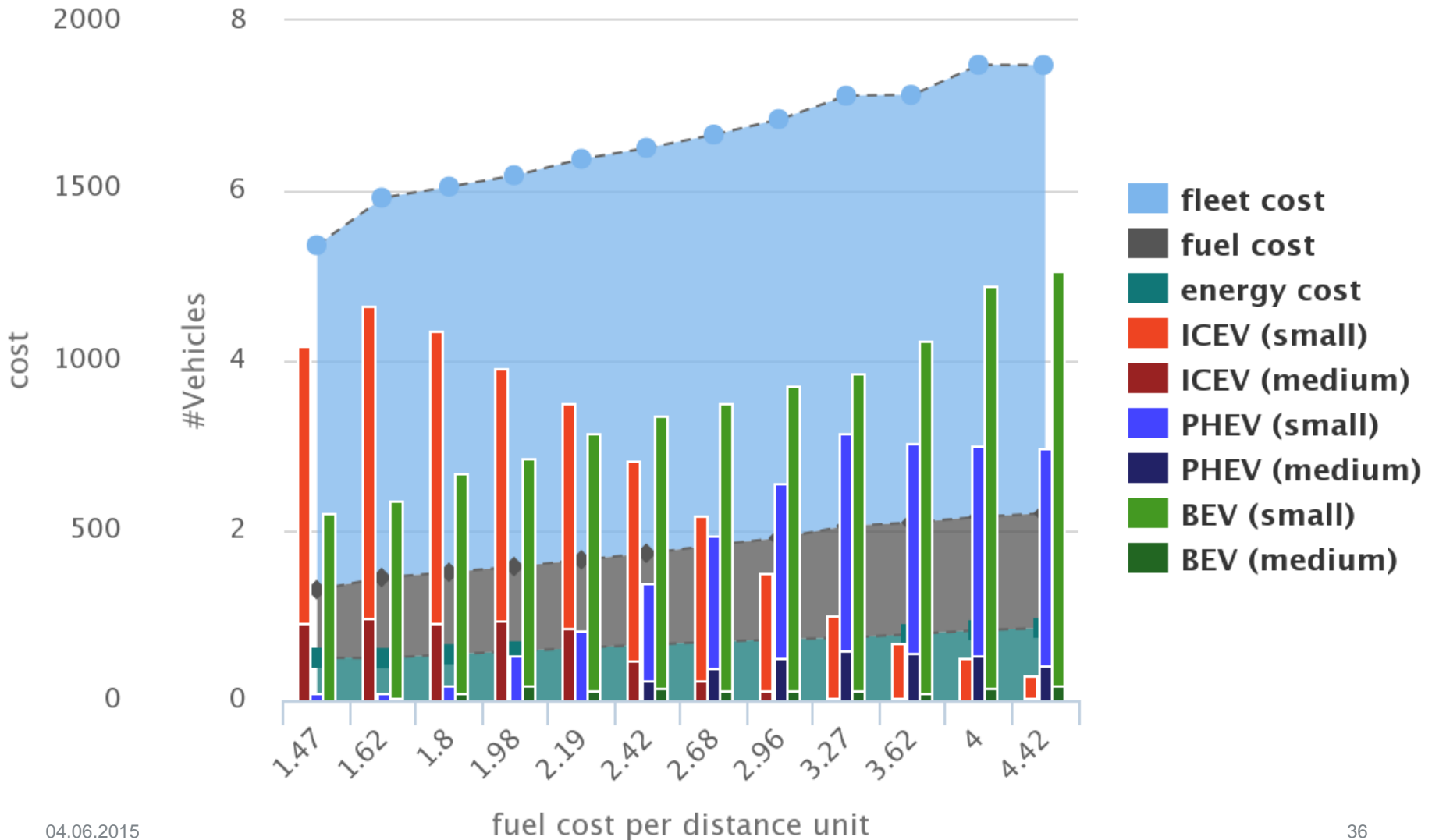
- Based on the E-VRPTW instances by Schneider et al. (2014)
- Extended by additional fleet configuration file
  - 2 vehicles per class (ICEV,PHEV,BEV) – one small, one medium sized
  - parameters based on Fraunhofer study (Plötz et al. 2013)
    - daily utility cost
      - (acquisition cost – reselling gain)
      - maintenance
      - driver wage
    - capacity and consumption
      - only relative values (based on the study)
      - actual values depend on the E-VRPTW instance

## Preliminary Experiments – Fleet Configuration

- Parameters from the E-VRPTW instance files:
  - load capacity  $C$
  - battery capacity  $Q$
  - energy consumption  $r$
  
- Fleet configuration:

| class   | ICEV       |            | PHEV       |            | BEV        |            |
|---------|------------|------------|------------|------------|------------|------------|
| type    | S          | M          | S          | M          | S          | M          |
| load    | $0.8 * C$  | $1.0 * C$  | $0.8 * C$  | $1.0 * C$  | $0.8 * C$  | $1.0 * C$  |
| fuel    | $0.23 * r$ | $0.28 * r$ | $0.26 * r$ | $0.33 * r$ | 0.0        | 0.0        |
| battery | 0.0        | 0.0        | $0.29 * Q$ | $0.42 * Q$ | $0.83 * Q$ | $1.0 * Q$  |
| energy  | 0.0        | 0.0        | $0.84 * r$ | $1.03 * r$ | $0.90 * r$ | $1.10 * r$ |
| cost    | 155        | 163        | 158        | 170        | 157        | 167        |

# Avg. Vehicle Class Usage



# Summary

- Fleet Mixing Problem with ICEV, PHEV and BEV
  
- Methodology
  - Modular design for handling problem specific sequence attributes
  - Labelling to use well-studied neighbourhoods directly
    - may be time consuming
    - can be replaced with other (greedy) procedure without modifying the neighbourhood operators
  - Directly applicable in a competitive metaheuristic framework
  
- Results
  - higher fuel prices => more electric vehicles
  - lower fixed cost still a major advantage of ICEVs

## Future work

- Instances using real street graphs
  - to better reflect urban settings
  
- Analysis of the metaheuristic components
  - contribution of set-partitioning, LNS and crossover
  - heuristic and exact labelling
  
- Introducing City Center restrictions
  - prohibited / restricted use of fossil fuel to travel from / to a customer in the center
  - promotes the use of (hybrid) electric vehicles
  - more on this topic at the VeRoLog 2015

**Thank you for your attention!**

## Acknowledgement

This work is partially funded by the Austrian Climate and Energy Fund within the "Electric Mobility Flagship Projects" program under grant 834868 (project VECEPT).





## References

- (Schneider et al., 2014) Schneider M, Stenger A, and Goeke D. The electric vehicle routing problem with time windows and recharging stations. *Transportation Science*, 48(4):500-520.
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- (Shaw 1997) Shaw P. Using constraint programming and local search methods to solve vehicle routing problems. Maher MJ, Puget JF, eds. *Proceedings of the 4th International Conference on Principles and Practice of Constraint Programming*. CP '98, (Springer, UK) 417-431.
- (Liu & Shen 1999) Liu F-H and Shen S-Y. The Fleet size and mix vehicle routing problem with time windows. *The Journal of the Operational Research Society*, 50(7):721-732.

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- (Plötz et al. 2013) *Markthochlaufszzenarien für Elektrofahrzeuge*. Karlsruhe : Fraunhofer ISI, 2013.

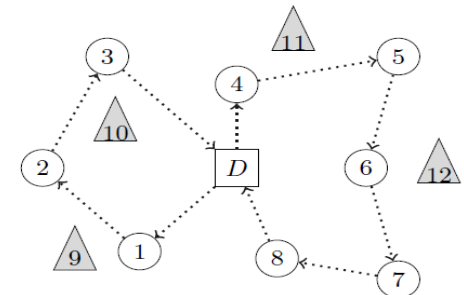
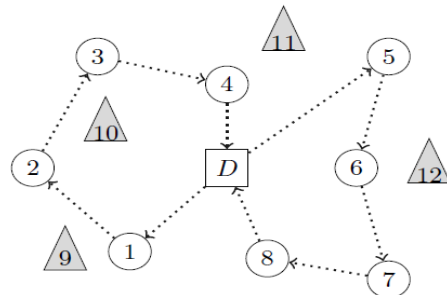
# Additional Slides

# Implicit handling of Recharging Stations

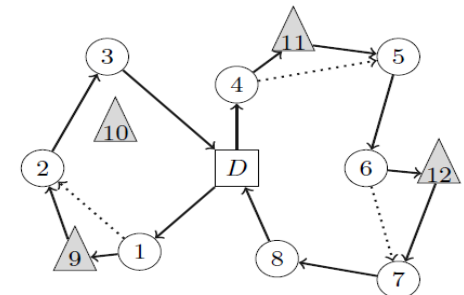
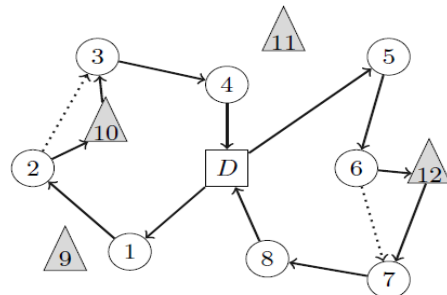
## Neighbourhood Search: Relocation Operator

| $i$ | $dist_{0,i}$ | $dist_{i-1,i}$ |
|-----|--------------|----------------|
| 1   | 4            | /              |
| 2   | 4            | 3              |
| 3   | 5            | 5              |
| 4   | 2            | 4              |
| 5   | 4            | 3              |
| 6   | 3            | 3              |
| 7   | 5            | 3              |
| 8   | 3            | 3              |

$dist_{i,j} = dist_{j,i}$   
other distances =  $\infty$



RELOCATE  
4 before 5



| $i \setminus j$ | $dist_{i,j}$ |    |    |    |
|-----------------|--------------|----|----|----|
|                 | 9            | 10 | 11 | 12 |
| 0               | 5            | 4  | 3  | 6  |
| 1               | 2            | 5  | /  | /  |
| 2               | 3            | 3  | /  | /  |
| 3               | /            | 3  | 5  | /  |
| 4               | /            | 4  | 2  | /  |
| 5               | /            | /  | 2  | 3  |
| 6               | /            | /  | 4  | 2  |
| 7               | /            | /  | /  | 4  |
| 8               | 5            | /  | /  | 5  |

| $\sigma$                      | $dist(\sigma)$ |
|-------------------------------|----------------|
| (0, 1, 2, 10, 3, 4, 0)        | 19             |
| (0, 5, 6, 12, 7, 8, 0)        | 19             |
| (0, 1, 9, 2, 3, 0)            | 16             |
| (0, 4, 11, 5, 6, 12, 7, 8, 0) | 21             |

| other properties           |
|----------------------------|
| $tt_{i,j} = dist_{i,j}$    |
| $[e_i, l_i] = [0, \infty]$ |
| $Y = 10$                   |
| $r = 1.0, g = 1.0$         |